

## Decimal - base 10 place values

and so on...	10000	1000	100	10	1
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so...  $156_{10} = (1 \times 100) + (5 \times 10) + (6 \times 1)$

## Binary - base 2 place values

\* 8 bits - 1 byte of data

and so on...	128	64	32	16	8	4	2	1
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## Hexadecimal - base 16 place values

and so on...	65536	4096	256	16	1
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**0x** - a prefix you might see sometimes to indicate the number is in hexadecimal rather than in some other base. The C programming language, and others, use it to tell the compiler "this is hex, not some meaningless letters and numbers."

One way (and probably the easiest way) to convert a number from decimal to hex is to convert it to binary first

**Subscripts:** 2, 8, 10, 16 - The base subscripts are used to indicate the type of number systems (binary, octal, decimal, hexadecimal)

### BASE 10

0  
1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12  
13  
14  
15

### BASE 16

0  
1  
2  
3  
4  
5  
6  
7  
8  
9  
A  
B  
C  
D  
E  
F

It always helps to draw out a chart for the number system when working with conversions

**Binary (base 2)**

0, 1

128	64	32	16	8	4	2	1	(place values)
0	0	0	0	0	0	0	0	

**Decimal (base 10)**

0, 1, 2, 3, 4, 5, 6, 7, 8, 9

10000000	1000000	100000	10000	1000	100	10	1	(place values)
0	0	0	0	0	0	0	0	

**Hexadecimal (base 16)**

0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15

65536	4096	256	16	1	(place values)
0	0	0	0	0	

**Decimal to Binary:**

work left to right and deduct the decimal amounts as you go - turn the values “on” for the correct places

so...  $156_{10} = 128 + 16 + 8 + 4 = 1001\ 1100_2$

$14_{10} = 8 + 4 + 2 = 0000\ 1110_2$

$28_{10} = 16 + 8 + 4 = 0001\ 1100_2$

## Binary to Hex:

Let's take those same binary numbers and turn them into hex

- when looking at binary you break each set of 4 bits into a single hex value
- remember that 4 bits can only hold up to a  $15_{10}$

$$\text{so... } 156_{10} = 1001\ 1100_2 = 9 + C = 9C_{16}$$

$$14_{10} = 0000\ 1110_2 = 0 + E = 0E_{16}$$

$$28_{10} = 0001\ 1100_2 = 1 + C = 1C_{16}$$

## Hex to Binary:

Each Hex digit is equal to 4 bits - use the values for the lowest set of bits (8, 4, 2, 1)

so...

$$6D_{16} = 0110\ 1101_2 = 109_{10}$$

let's test this out:

$$\text{hex: } (6 * 16) + (13 * 1) = 96 + 13 = 109_{10}$$

$$\text{binary: } 64 + 32 + 8 + 4 + 1 = 109_{10}$$

$$C5_{16} = 1100\ 0101_2 = 197_{10}$$

let's test this out:

$$\text{hex: } (12 * 16) + (5 * 1) = (192 + 5) = 197_{10}$$

$$\text{binary: } 128 + 64 + 4 + 1 = 197_{10}$$

$$56_{16} = 0101\ 0110 = 86_{10}$$

let's test this out:

$$\text{hex: } (5 * 16) + (6 * 1) = (80 + 6) = 86_{10}$$

$$\text{binary: } 64 + 16 + 4 + 2 = 86_{10}$$